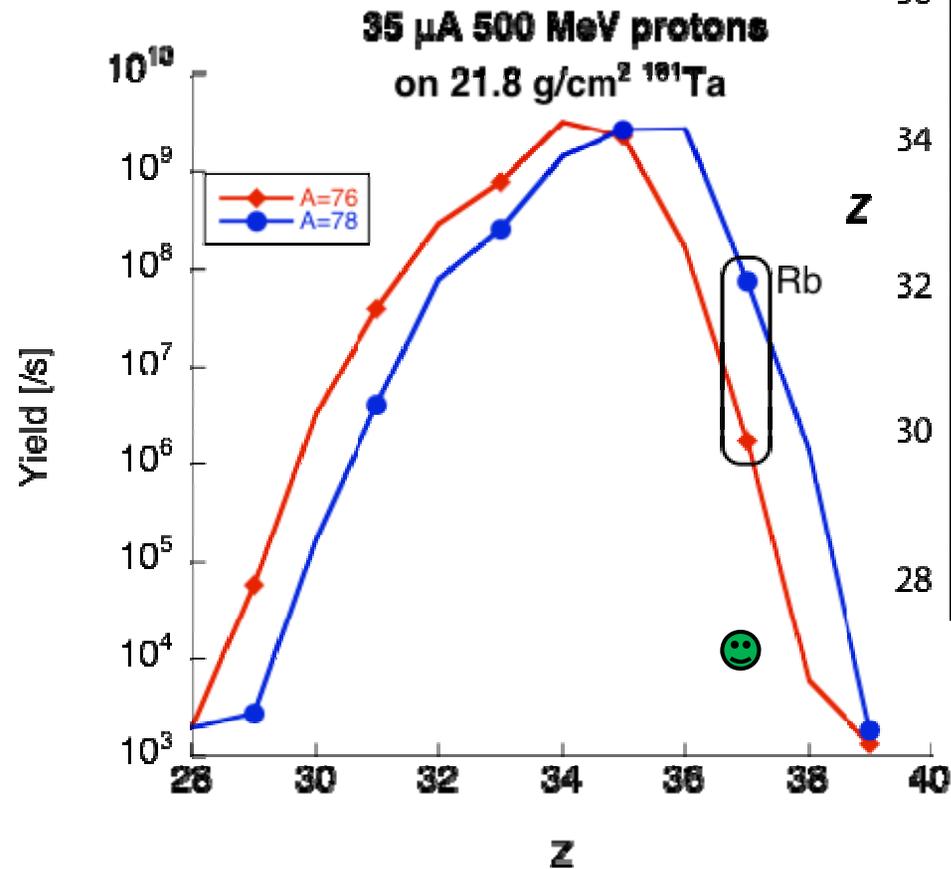
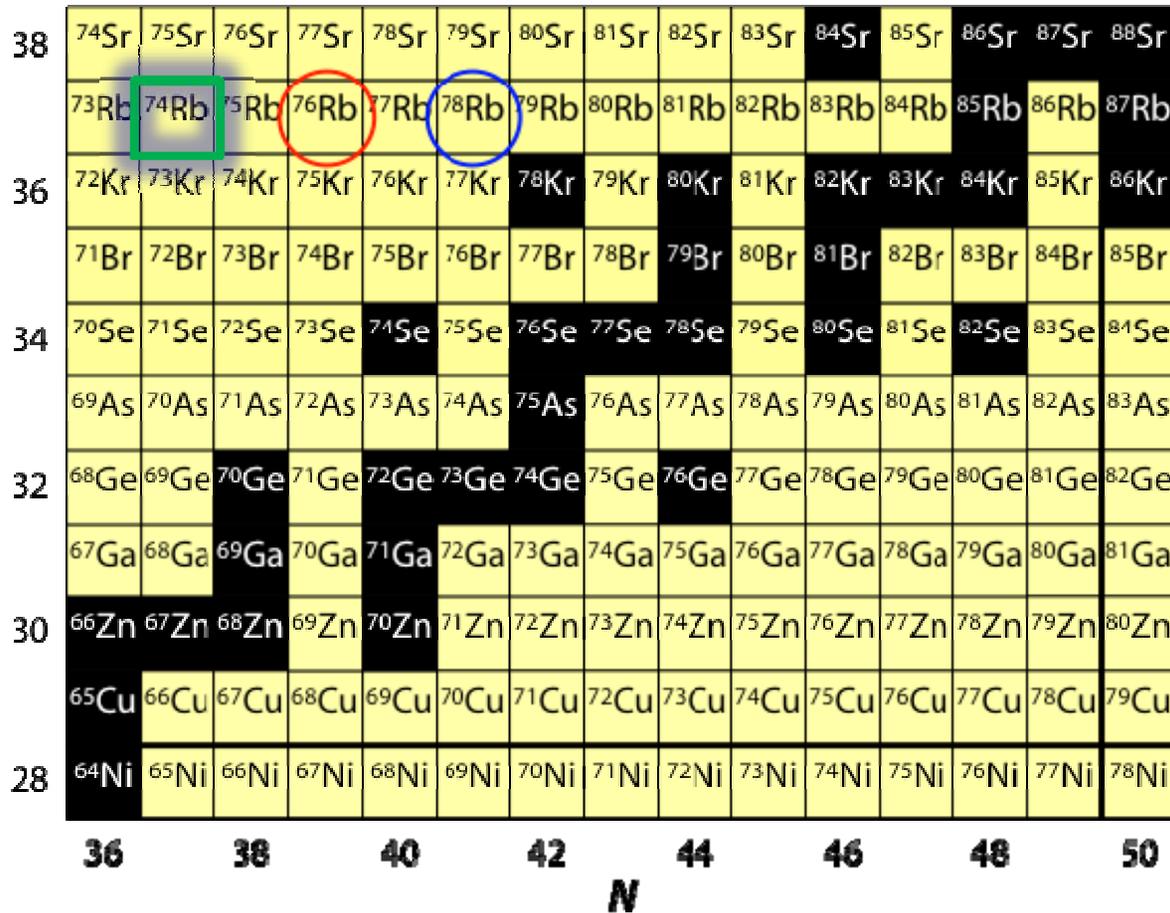


# High yields of rubidium isotopes are available with Nb, ZrC, or Ta targets at ISAC.

Nuclide	$T_{1/2}$	Nb (10 $\mu$ A)	ZrC (35 $\mu$ A)	Ta (35 $\mu$ A)
$^{74}\text{Rb}$	65 ms	$1.30 \times 10^4$	$4.20 \times 10^2$	
$^{76}\text{Rb}$	37 s	$*1.60 \times 10^7$	$5.30 \times 10^7$	$4 \times 10^4$
$^{78}\text{Rb}^g$	17.5 m	$7.00 \times 10^8$	$2.20 \times 10^9$	$1 \times 10^7$
$^{78}\text{Rb}^m$	5.7 m	$4.20 \times 10^9$	$6.90 \times 10^9$	$6 \times 10^7$
$^{80}\text{Rb}$	33 s	$2.60 \times 10^{10}$	$3.50 \times 10^{10}$	$1 \times 10^9$



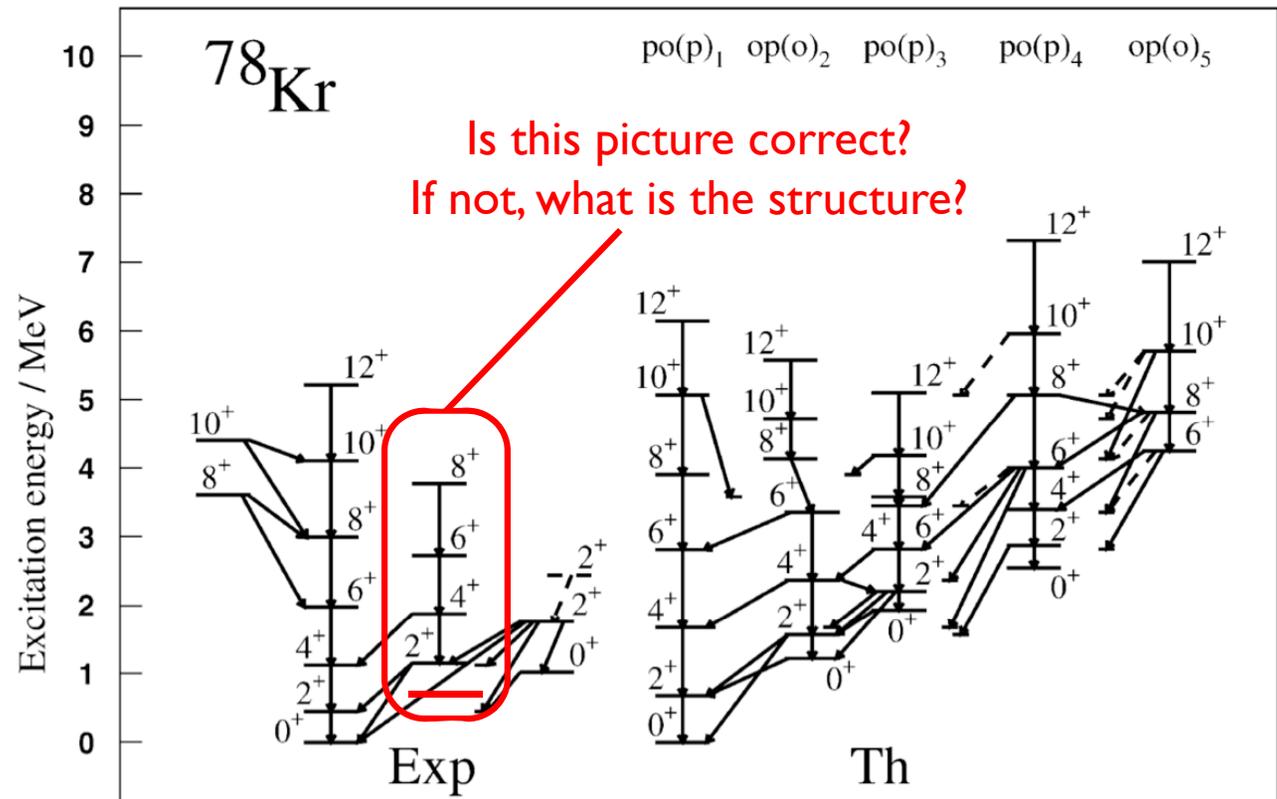
# SI215: Characterization of shape coexistence near $N=40$

Steve Yates

Representing **SI215**,  
a collaboration including:  
Georgia Tech, Guelph, SFU,  
TRIUMF, NSCL, and UK  
spokesman: W. D. Kulp  
(wdkulp@mailaps.org)

ISAC Forum

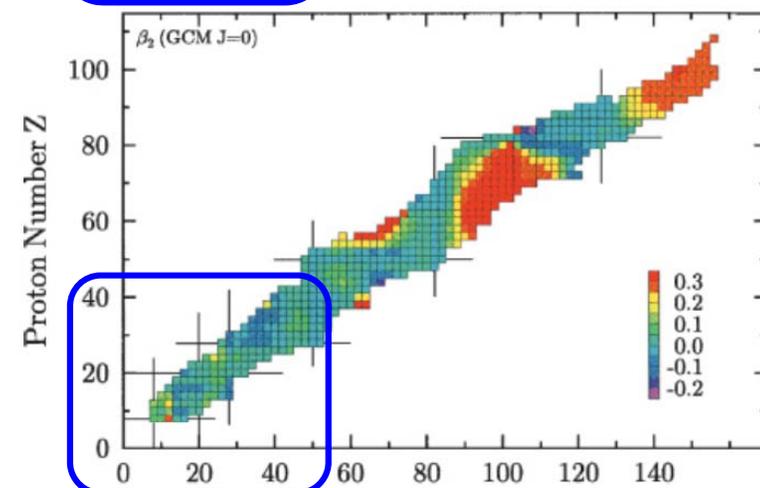
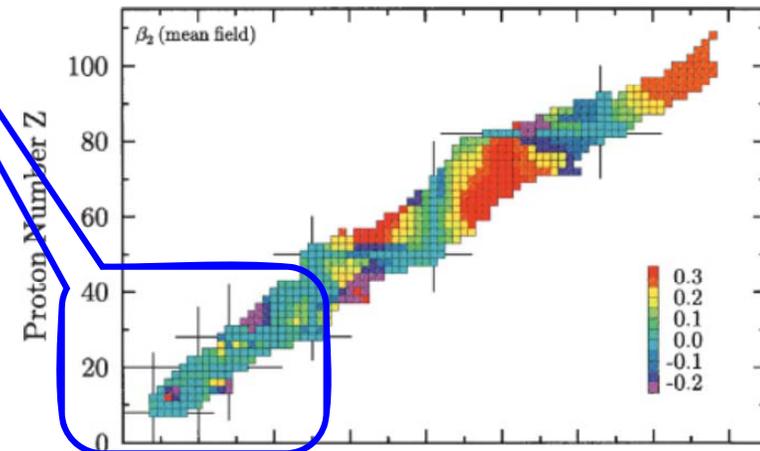
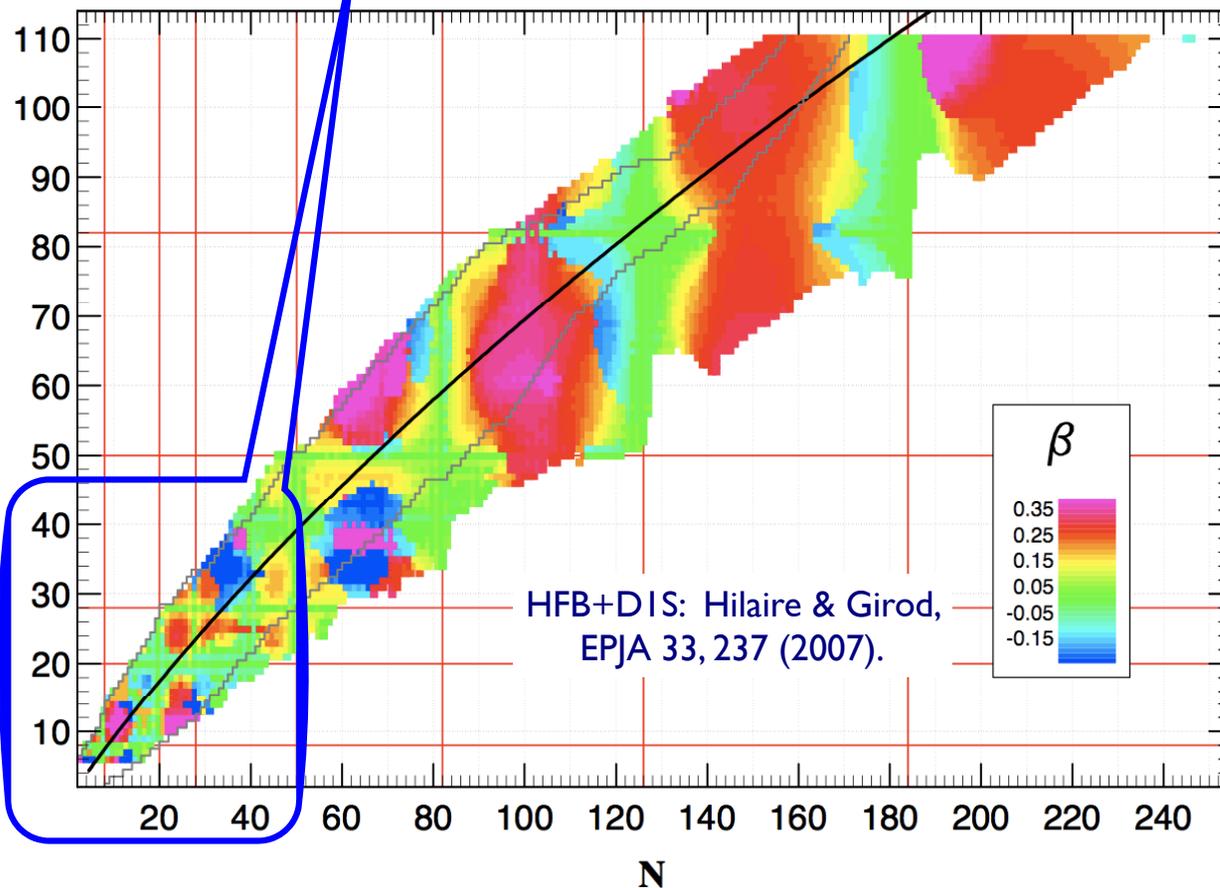
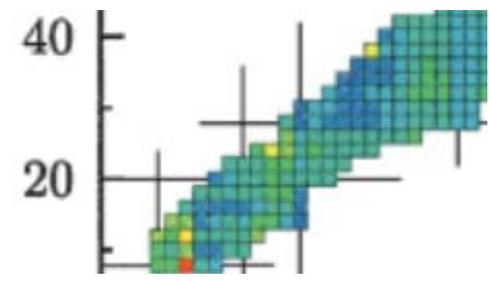
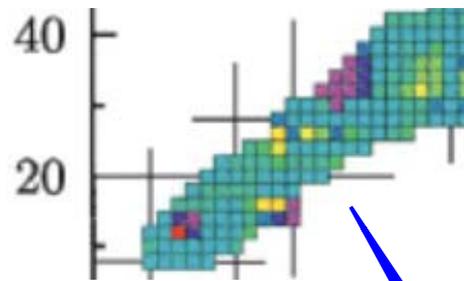
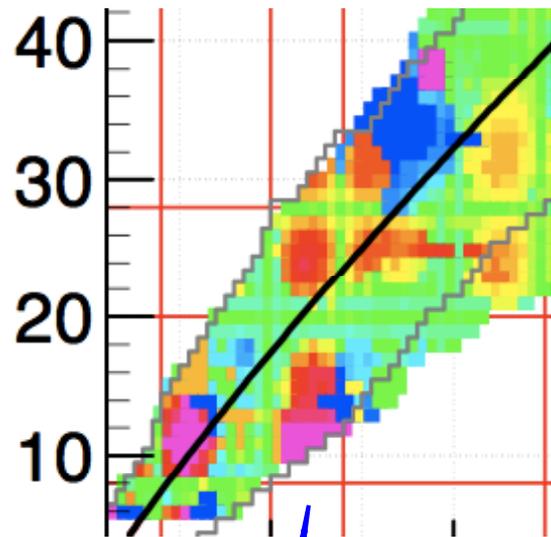
2 Dec 2009



Multi-step Coulomb excitation of  $^{78}\text{Kr}$  suggests that the  $2^+_2$  state belongs to a coexisting  $K=0$  oblate band, **the band-head of which has not yet been observed.**

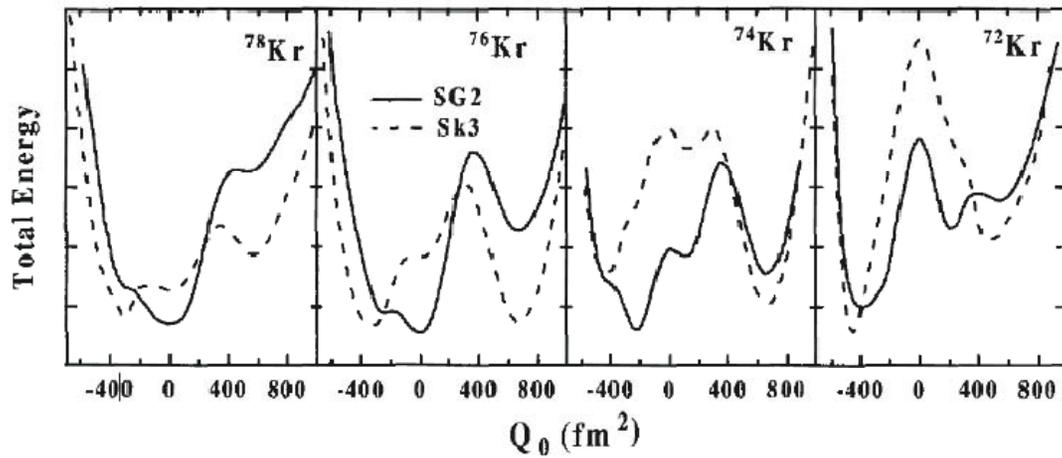
Becker et al., Nucl. Phys.A770, 107 (2006)

# Oblate-deformed shapes are predicted in the $A \sim 70$ region.

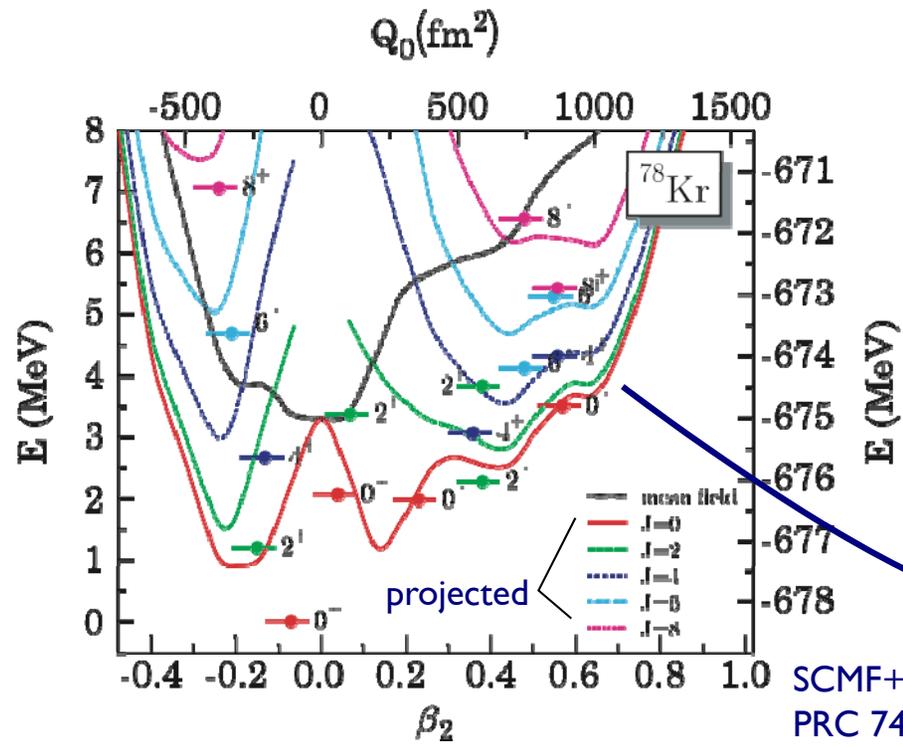
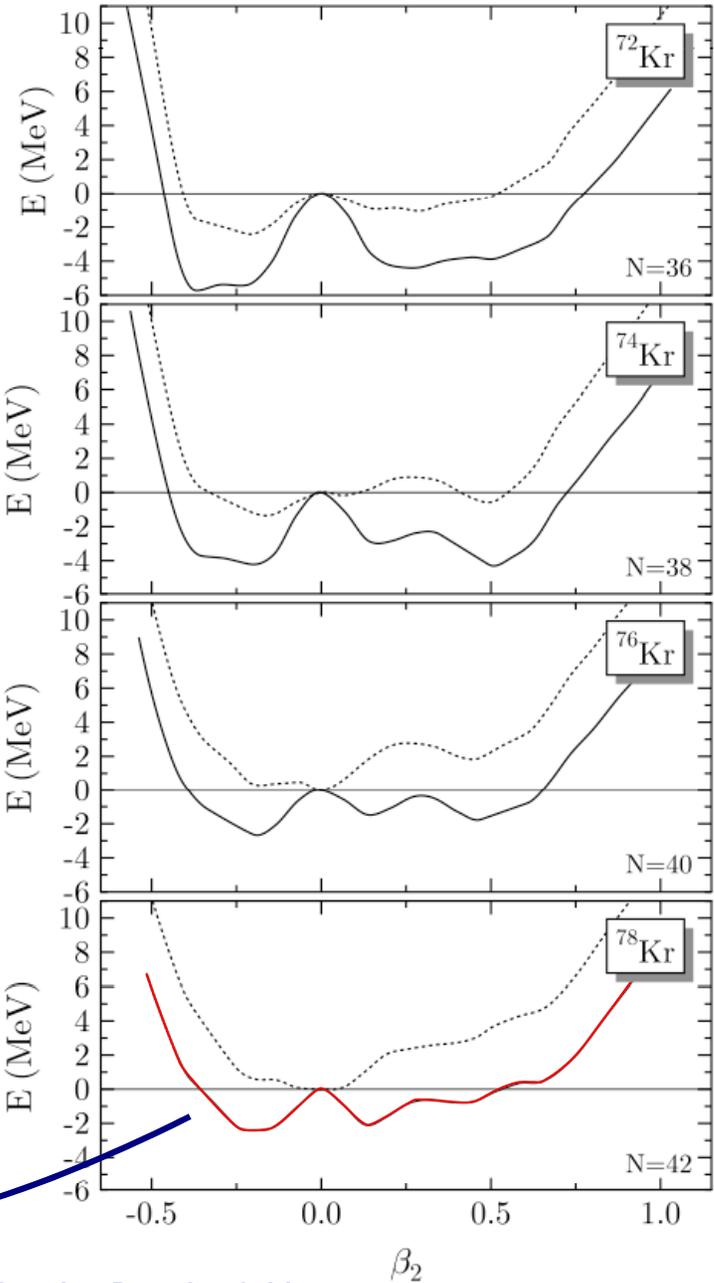


SCMF+Sly4 & GCM: Bender, Bertsch & Heenen, PRC 73, 034322 (2006).

# Mean-field calculations indicate coexisting oblate and prolate shapes in the krypton isotopes.



HF+BCS+Skyrme: Sarriguren, Moya de Guerra & Escuderos, NPA 658, 13 (1999).



SCMF+Sly6 & GCM: Bender, Bonche & Heenen, PRC 74, 024312 (2006).

# Strong $E0$ transitions are evidence of shape coexistence.

Monopole strength parameter

$$\rho_{if}(E0) = \frac{\langle f | \sum_j e_j r_j^2 | i \rangle}{eR^2} \equiv \frac{\langle f | m(E0) | i \rangle}{eR^2} \equiv \frac{M_{if}(E0)}{eR^2}$$

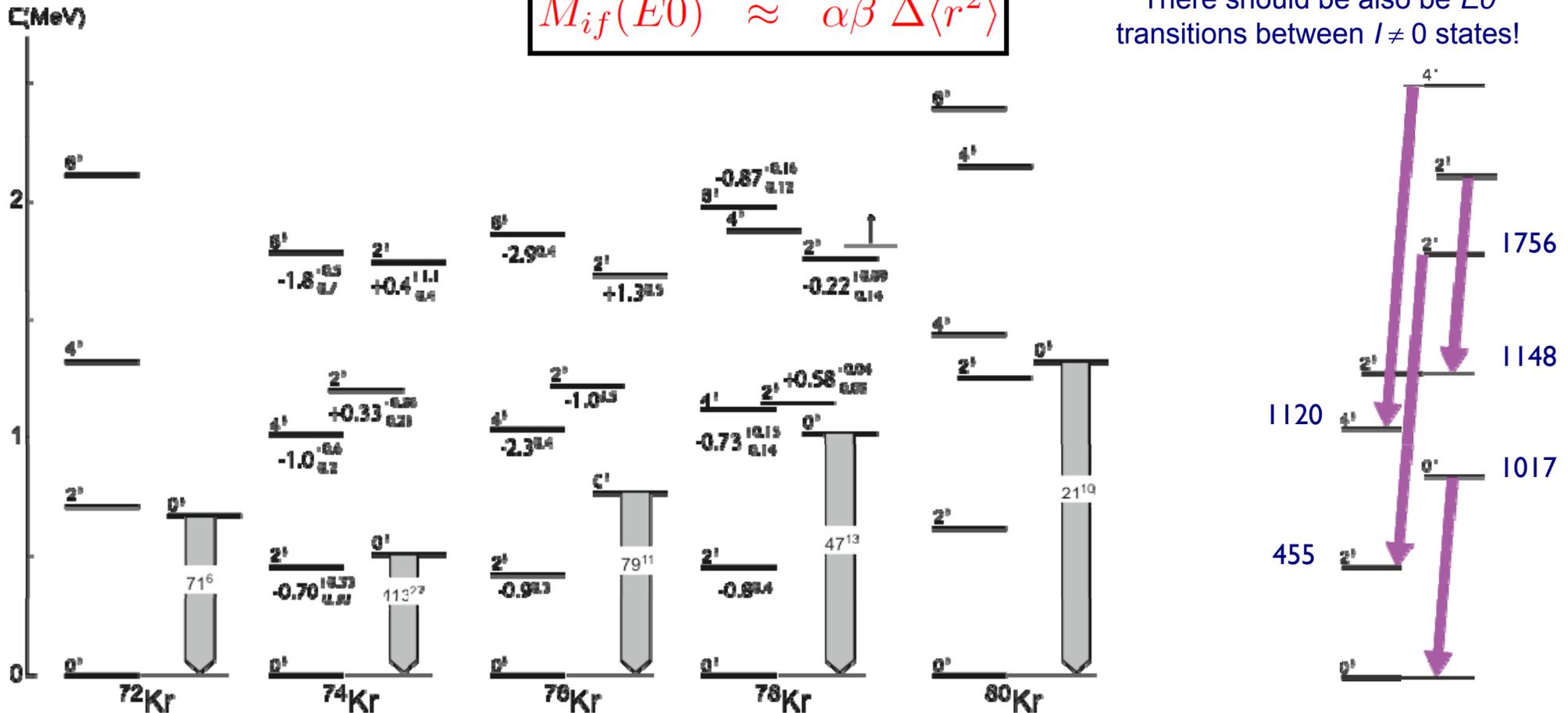
Monopole strength from mixing of states with different  $\langle r^2 \rangle$   $|i\rangle = \alpha|1\rangle + \beta|2\rangle$ ,  $|f\rangle = -\beta|1\rangle + \alpha|2\rangle$

$$M_{if}(E0) = \alpha\beta\{\langle 2 | m(E0) | 2 \rangle - \langle 1 | m(E0) | 1 \rangle\} + (\alpha^2 - \beta^2)\langle 1 | m(E0) | 2 \rangle$$

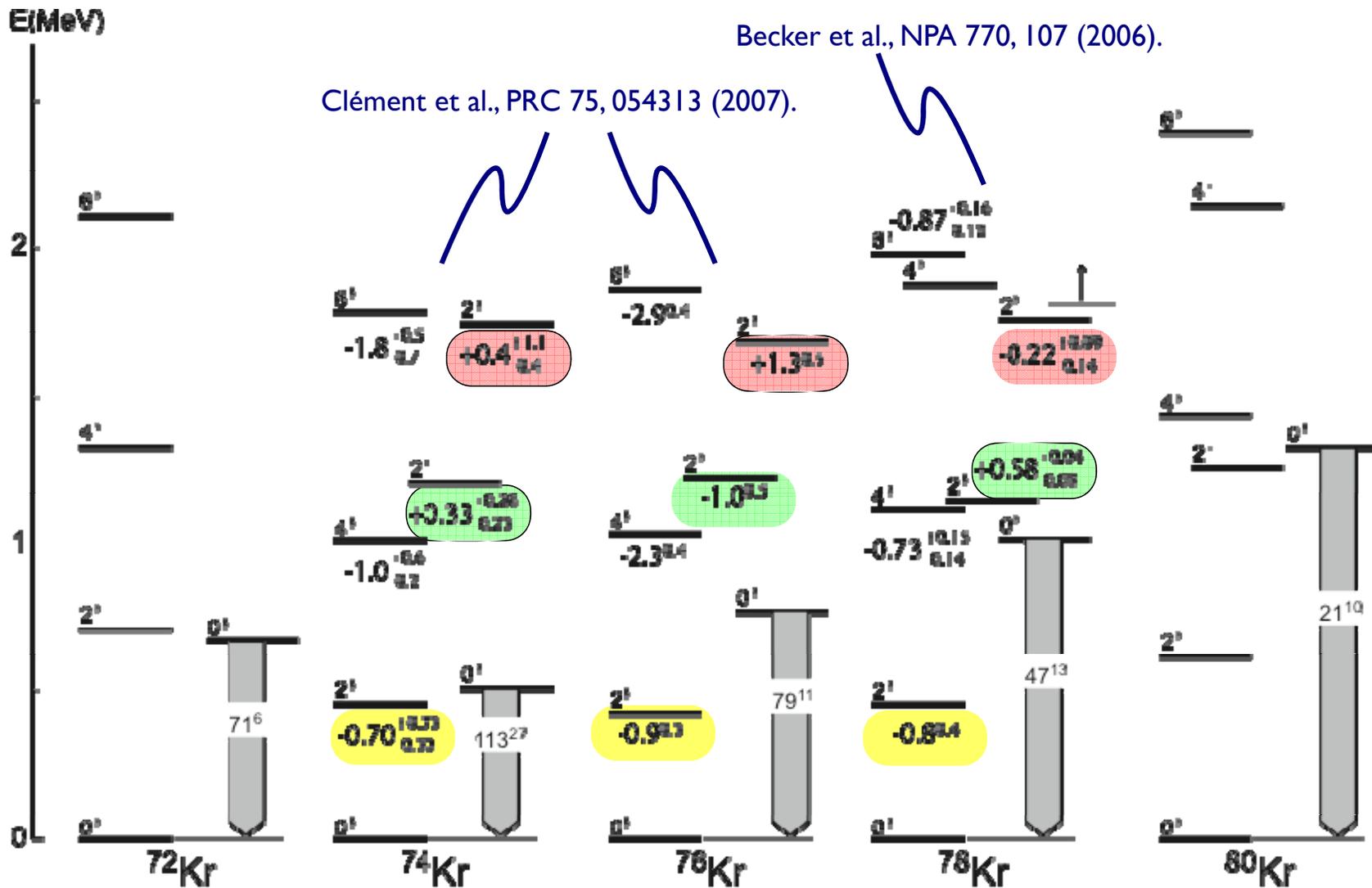
$$\Delta\langle r^2 \rangle \equiv -\langle 1 | \sum_j e_j r_j^2 | 1 \rangle + \langle 2 | \sum_j e_j r_j^2 | 2 \rangle$$

$$M_{if}(E0) \approx \alpha\beta \Delta\langle r^2 \rangle$$

There should be also  $E0$  transitions between  $l \neq 0$  states!



Recent multi-step Coulomb excitation studies support oblate and prolate coexistence in the light krypton isotopes.

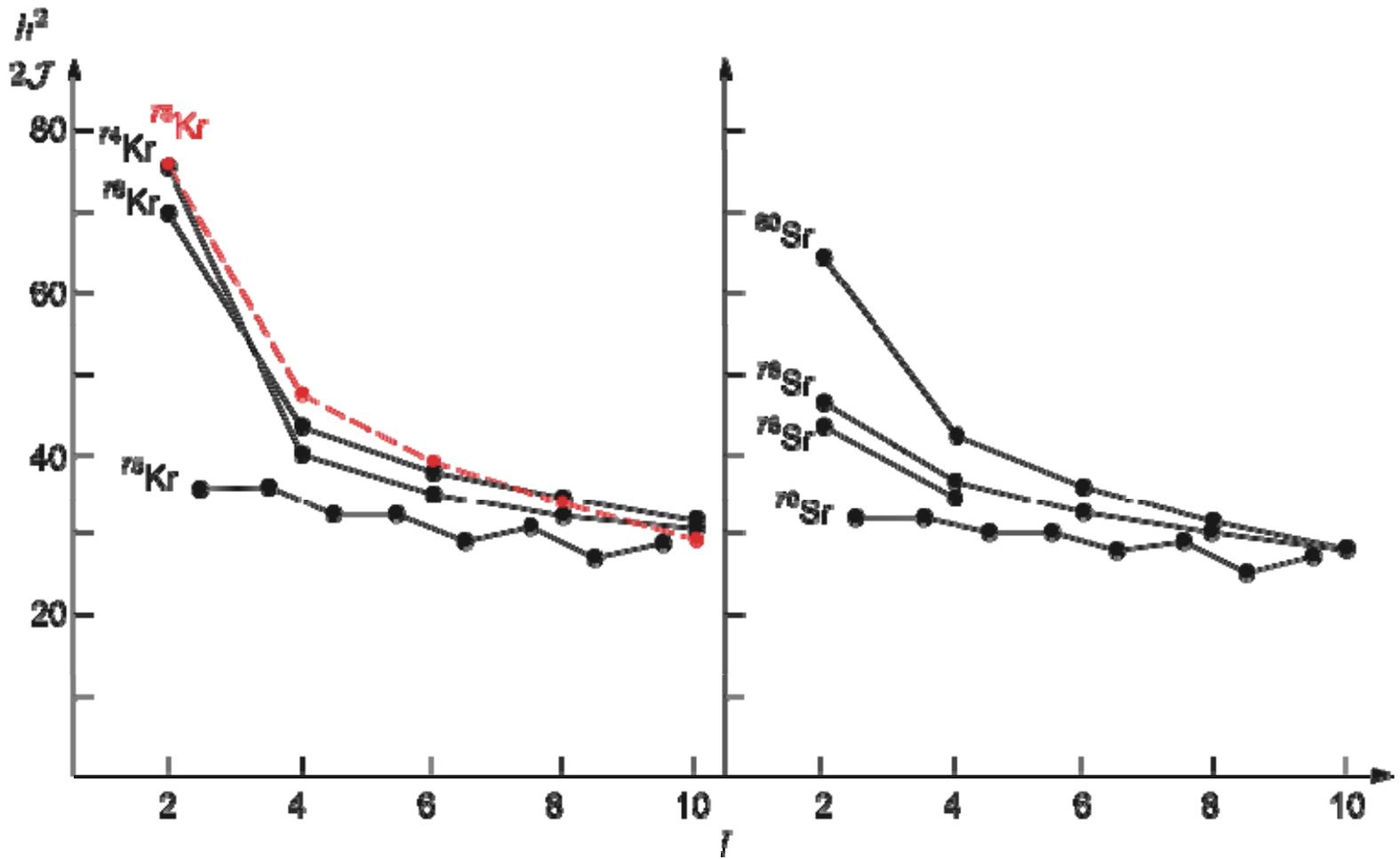


$$\langle KI_i || \mathcal{M}(E2) || KI_i \rangle = \sqrt{\frac{5}{16\pi}} (2I_i - 1)^{\frac{1}{2}} \langle I_i K 2 0 | I_i K \rangle e Q_0$$

The  $K$ -quantum number determines sign of the Clebsch-Gordan coefficient:

$$3K^2 - I(I+1) \rightarrow \mathbf{+6} \text{ for } (K=2, I=2), \quad \mathbf{-6} \text{ for } (K=0, I=2)$$

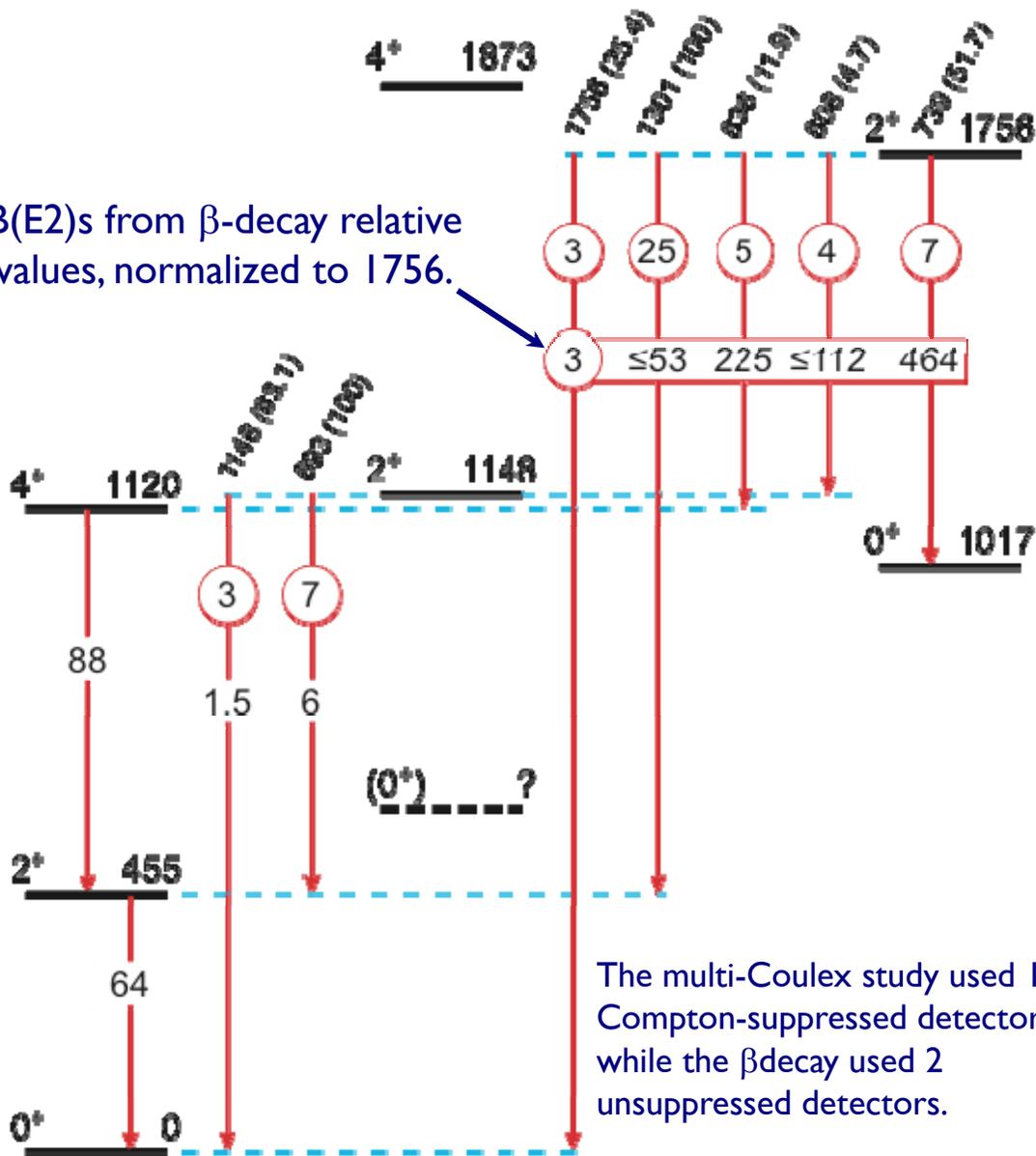
Large deviations from a constant rotational parameter at low spin indicate strong mixing between coexisting shapes.



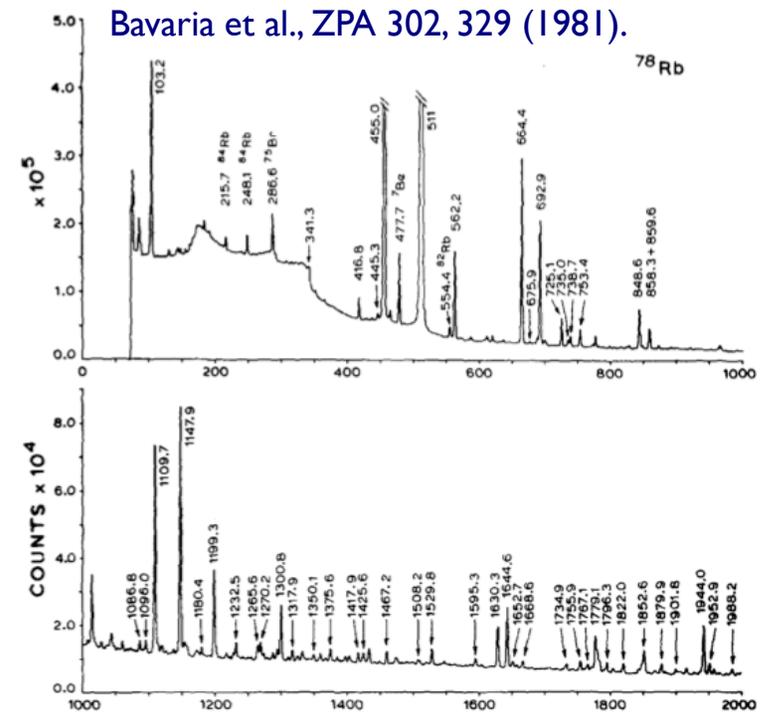
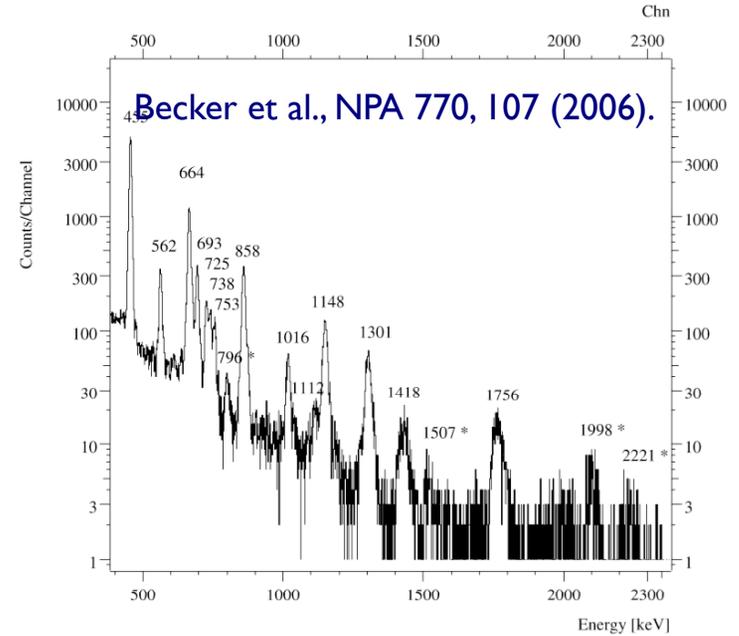


The multi-step Coulex study should provide a much cleaner picture of the structure, but the results do not agree with  $\beta$  decay measurements.

B(E2)s from  $\beta$ -decay relative values, normalized to 1756.

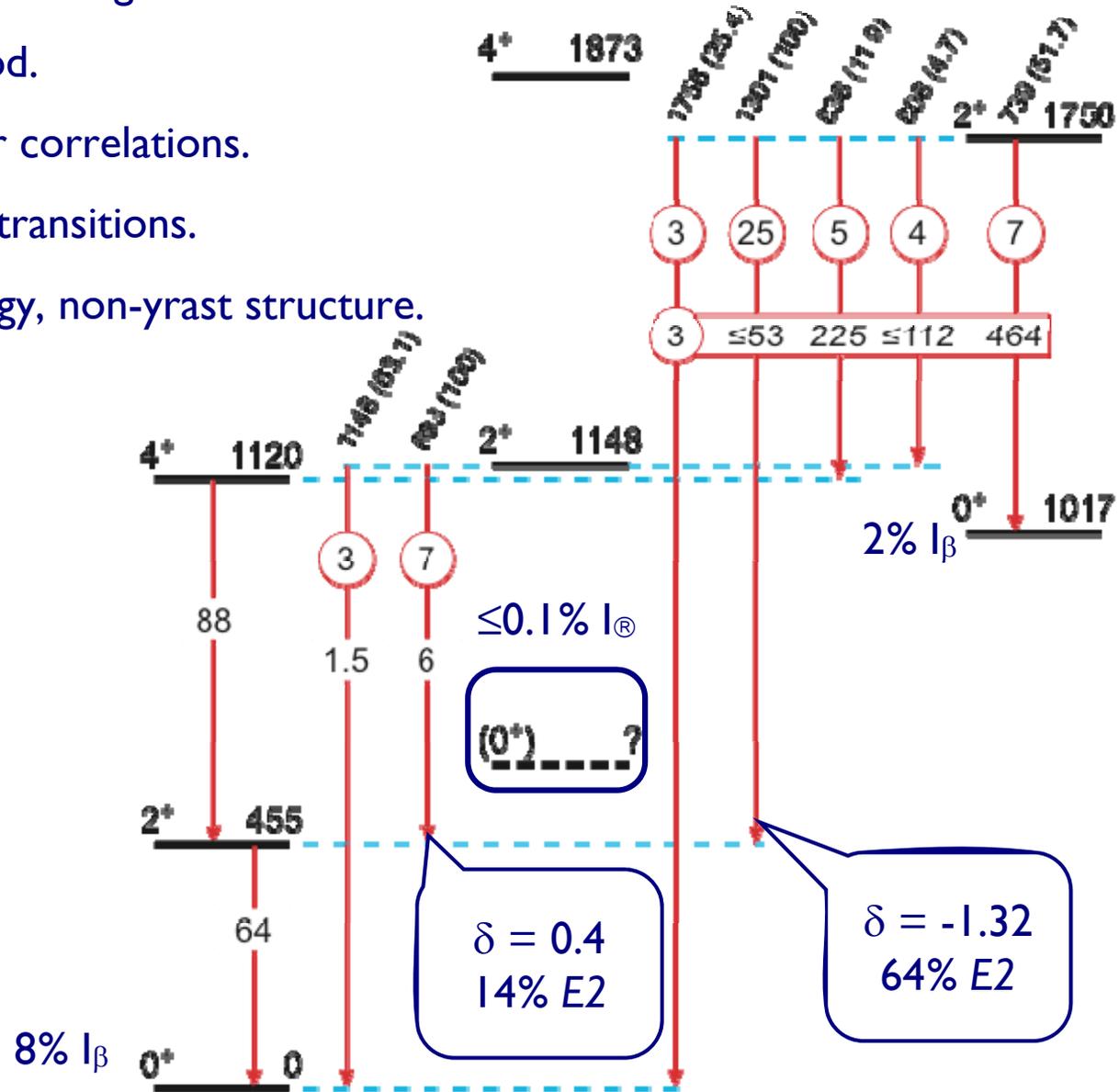


The multi-Coulex study used 12 Compton-suppressed detectors, while the  $\beta$  decay used 2 unsuppressed detectors.



The goal of SI215 was to investigate the nature of the coexisting bands near  $N=40$ .

- Search for  $0^+$  oblate bandhead or set a stringent upper limit on its population.
- Measure  $B(\lambda)$  values for transitions depopulating the 1756-keV level.
- Measure  $\alpha_K$  with normalized CE/ $\gamma$  method.
- Measure mixing ratios using  $\gamma\gamma(\theta)$  angular correlations.
- Determine  **$E0$  components** for  $I^\pi \rightarrow I^\pi$  transitions.
- Obtain detailed information on low-energy, non-yrast structure.
- $\gamma$ - $\gamma$ ,  $\gamma$ -CE, CE-CE spectroscopy.



# The $8\pi$ spectrometer

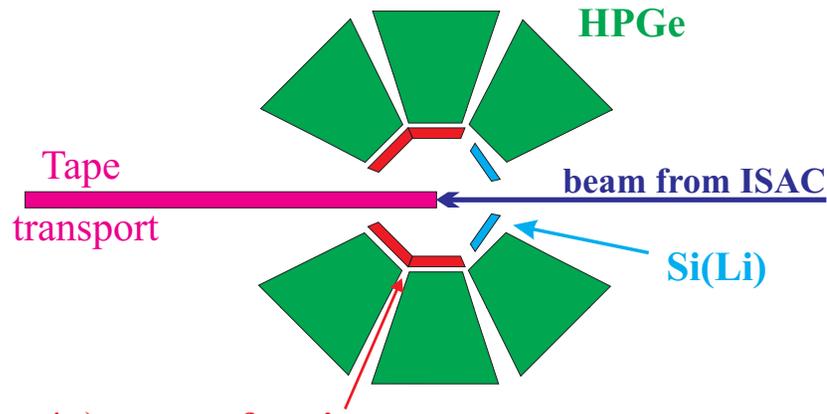
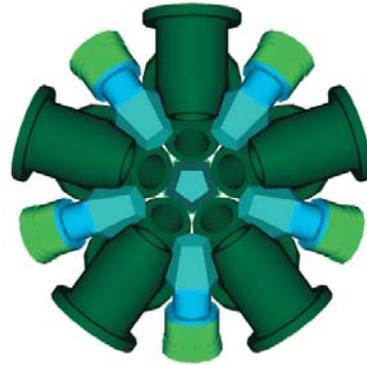
## $8\pi$ Spectrometer at ISAC

20 Compton-Suppressed HPGe detectors  
and 10 BaF2 detectors for  $\gamma$ -ray detection

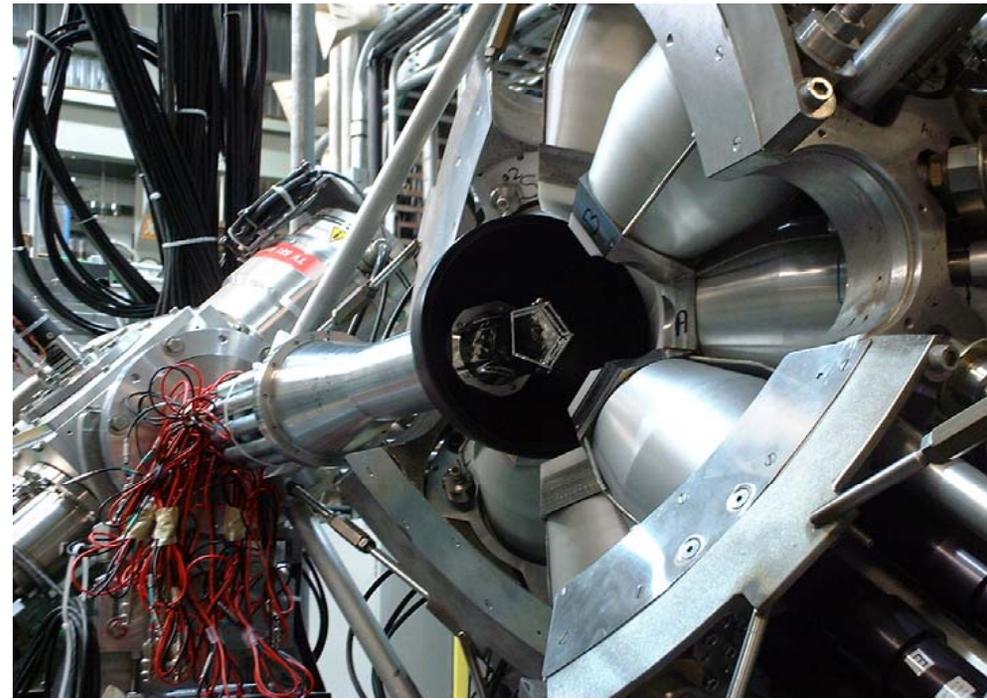
20 plastic scintillators for  $\beta$  detection

5 Si(Li) detectors for conversion electron spectroscopy

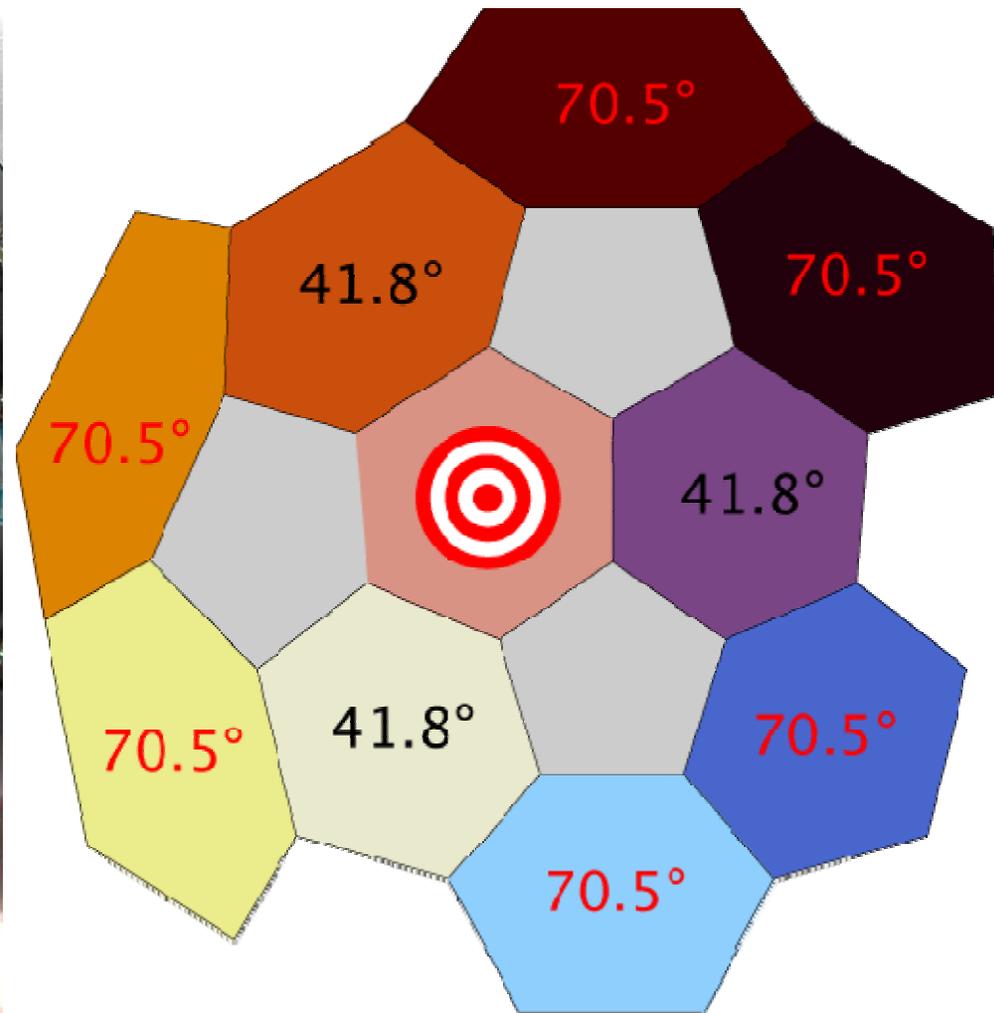
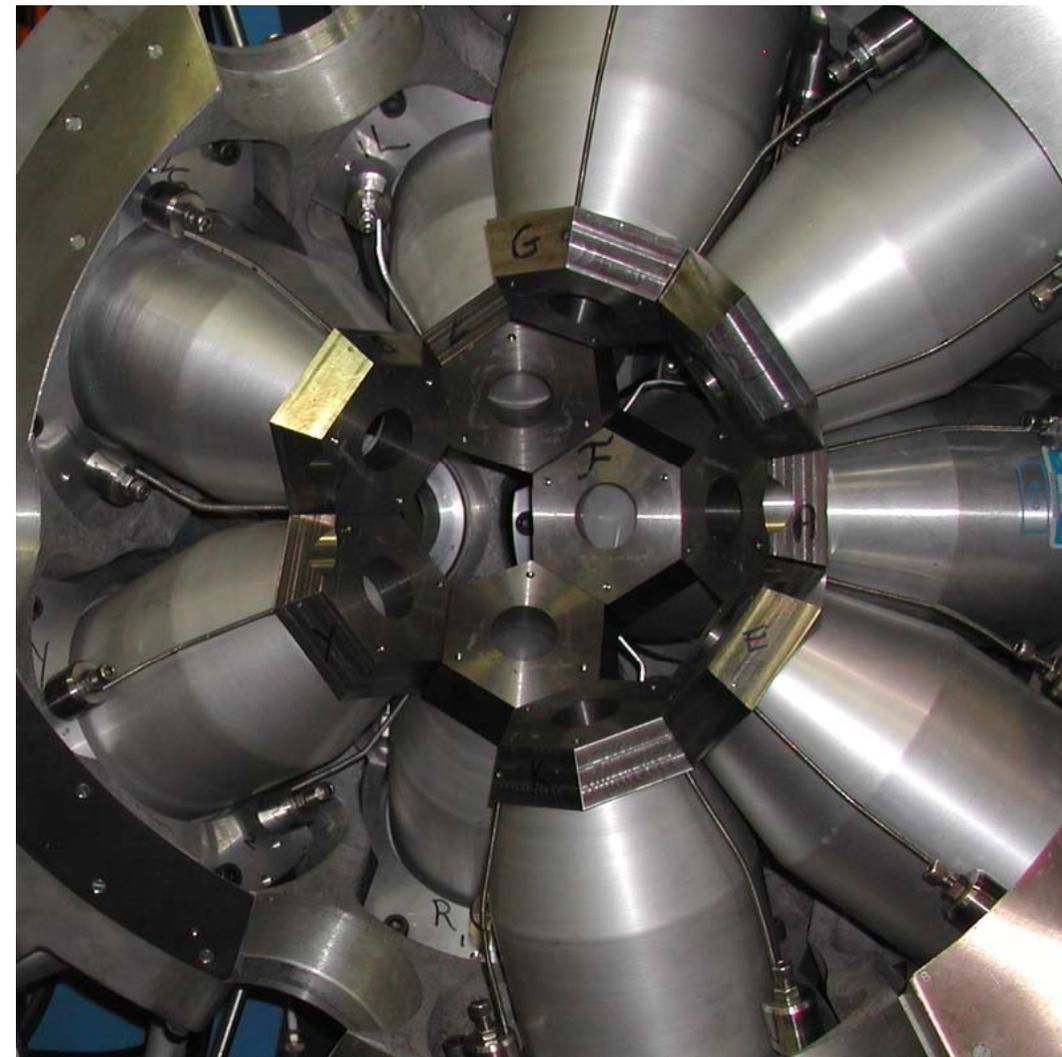
Fast, in-vacuum tape transport system



**2π (or 4π) array of positron counters**



# $8\pi$ Spectrometer



# Precision $\gamma$ - $\gamma$ angular correlation measurements

$$W(\theta) = N[1 + A_2 P_2(\theta) + A_4 P_4(\theta)]$$

$P_2(\theta)$ ,  $P_4(\theta)$  - Legendre polynomials

5 angles between detector pairs

41.8° (60 pairs)

70.5° (120 pairs)

109.5° (120 pairs)

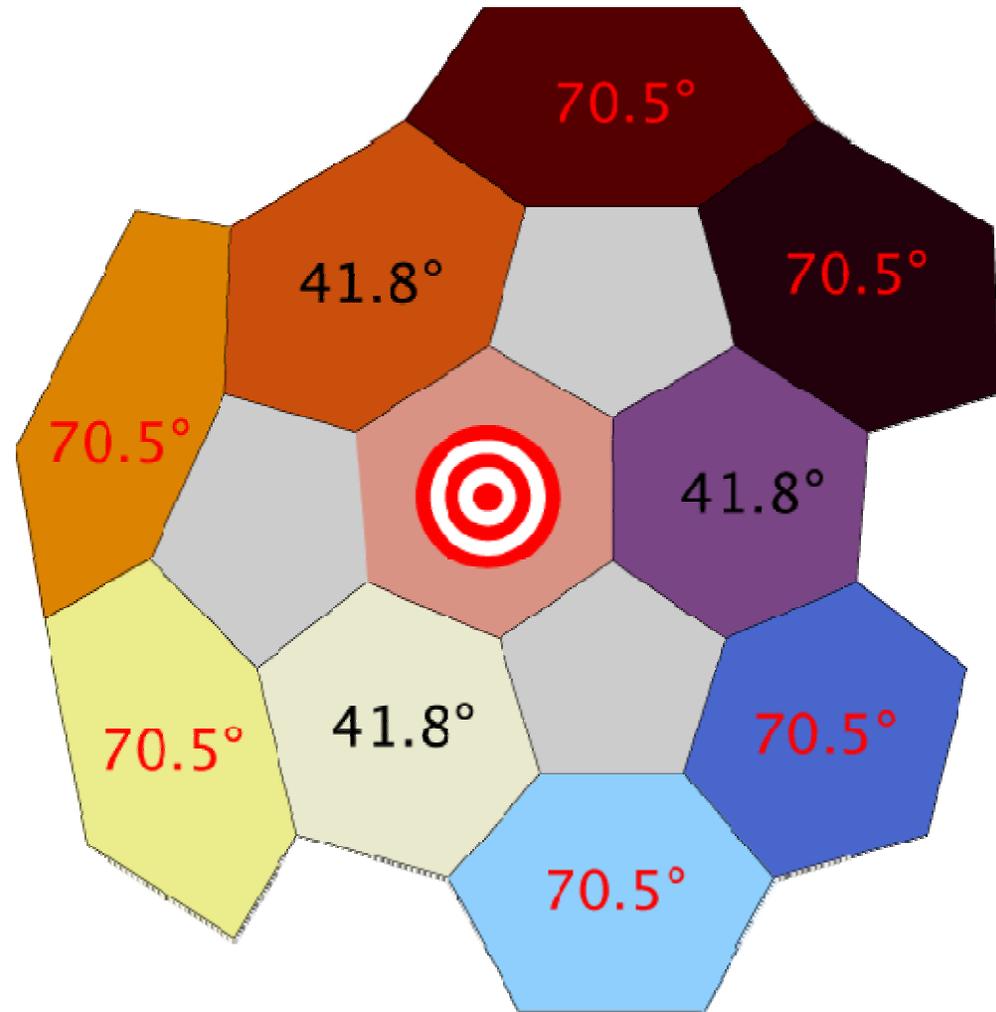
138.2° (60 pairs)

180° (20 pairs)

Small pairwise  $\gamma$ - $\gamma$  angular distortions

4 - 2 - 0 cascade: 0.57%

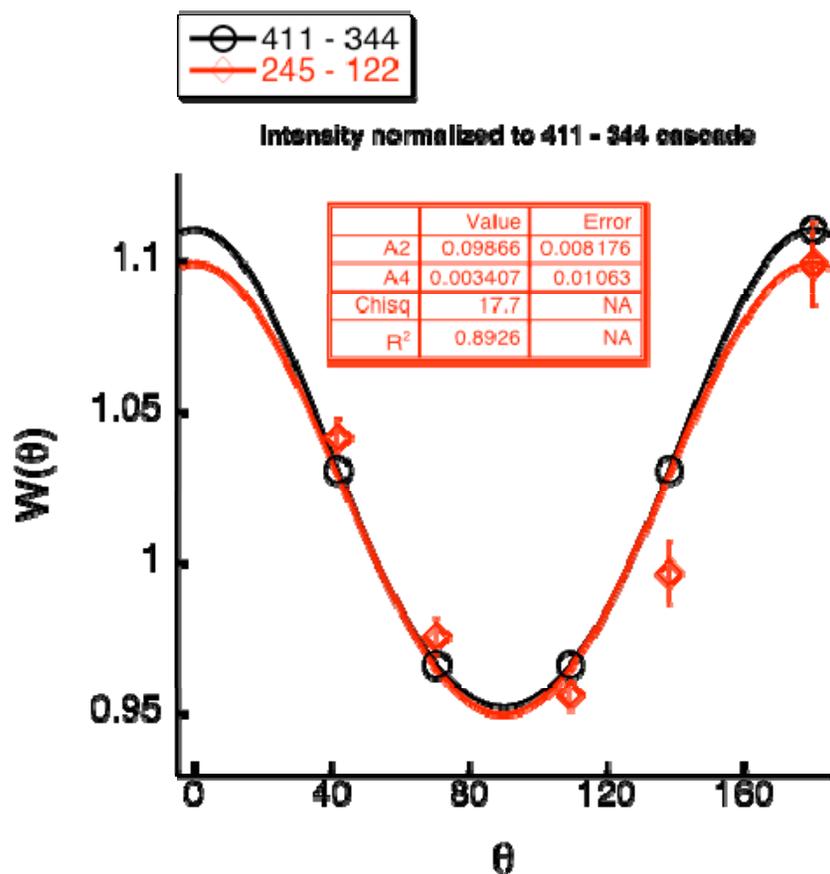
2 - 4 - 2 cascade: 1.50%



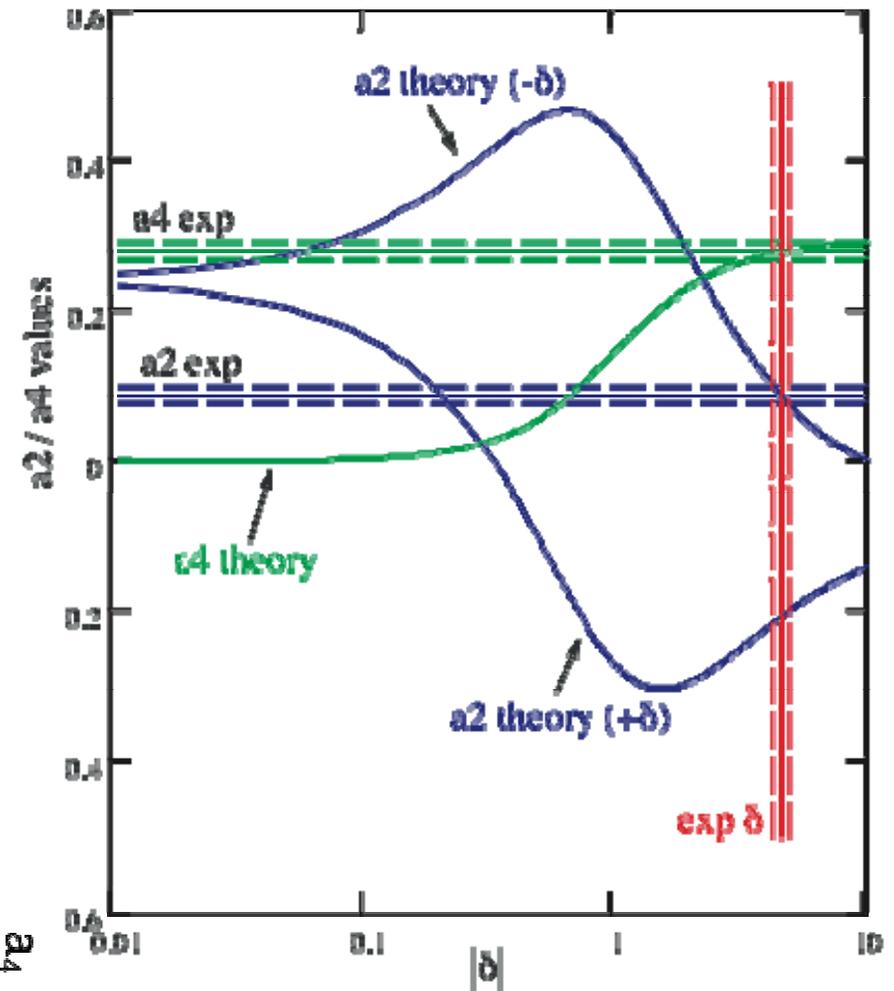
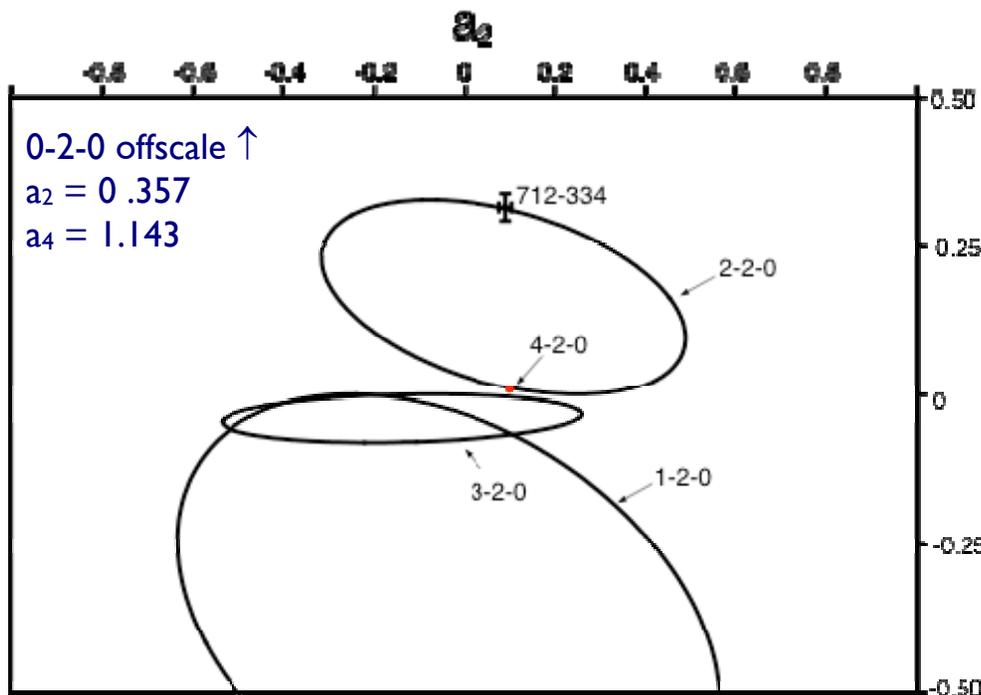
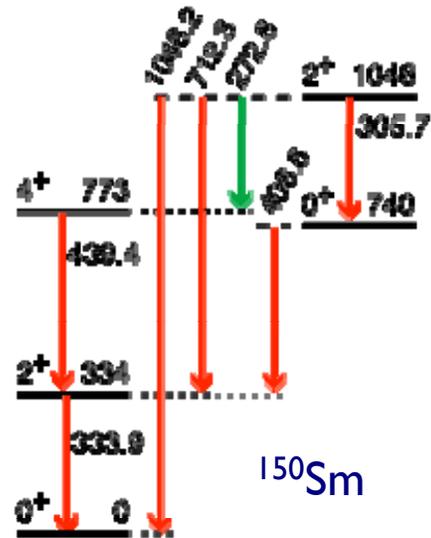
An internal normalization can be used to determine the multipolarity.

Correction factors for each angle are extracted using transitions of known multipolarity, e.g., a cascade of E2 transitions from levels of spin  $4^+ \rightarrow 2^+ \rightarrow 0^+$ .

Normalized in this way, the data from  $^{152}\text{Sm}$  closely fits the theoretical curve.

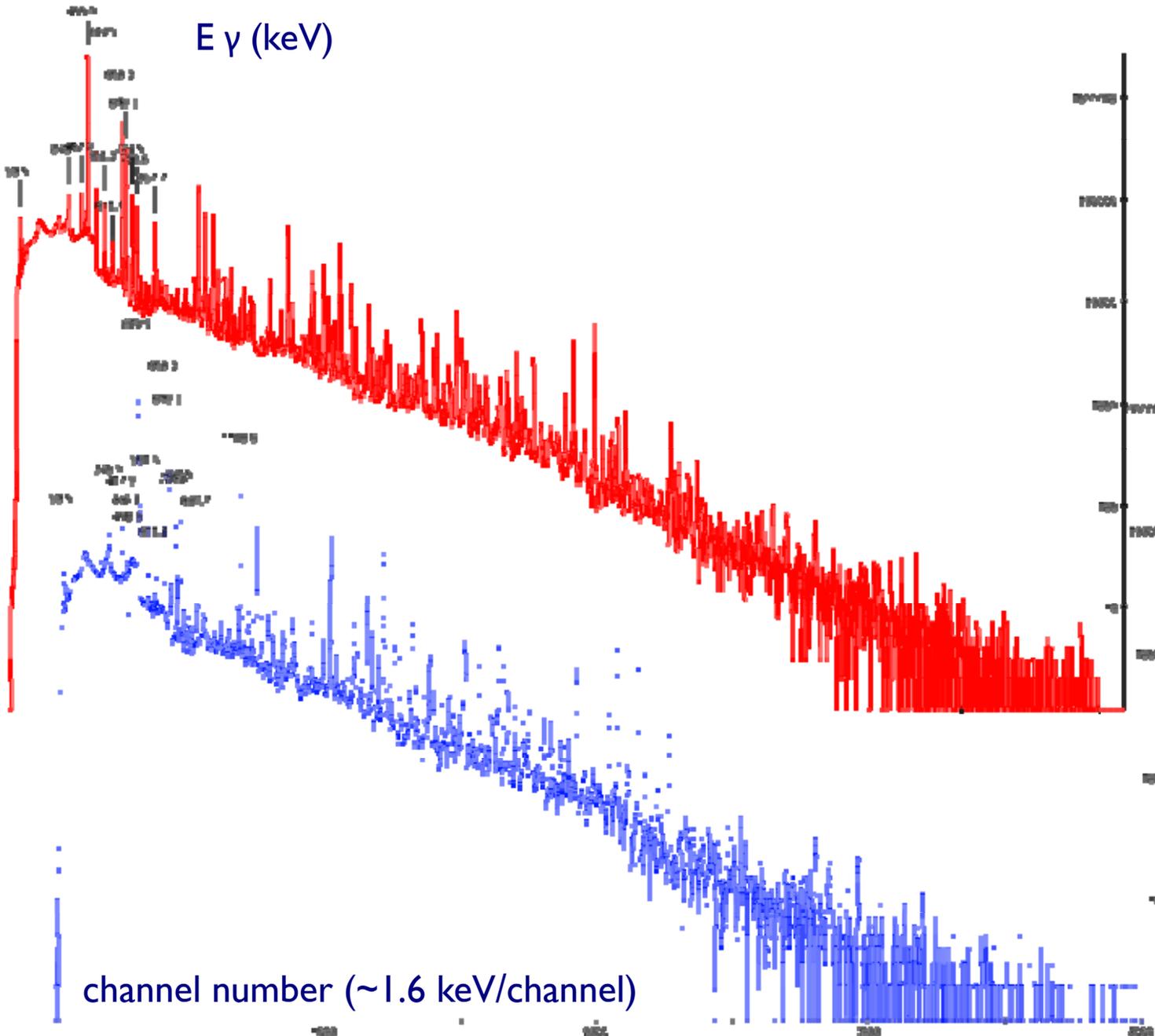


Precision  $\gamma\gamma(\theta)$  measurements can yield the sign of the multipole mixing ratio,  $\delta$ .



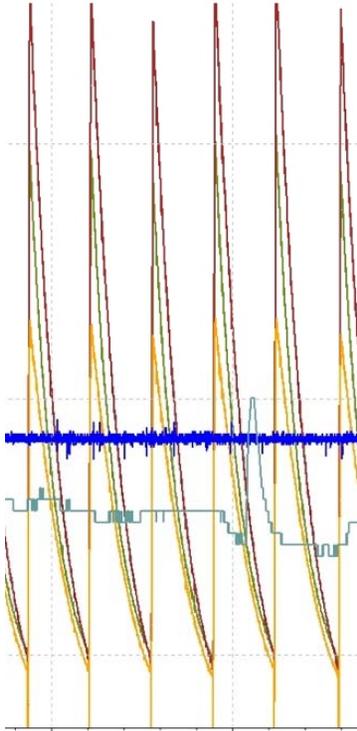
Ph. D. thesis work of P. Schmelzenbach, OSU.

The high  $\beta$ -decay Q value (7243 keV) leads to complex  $\gamma$ -ray spectra (a sign of things to come further from stability).

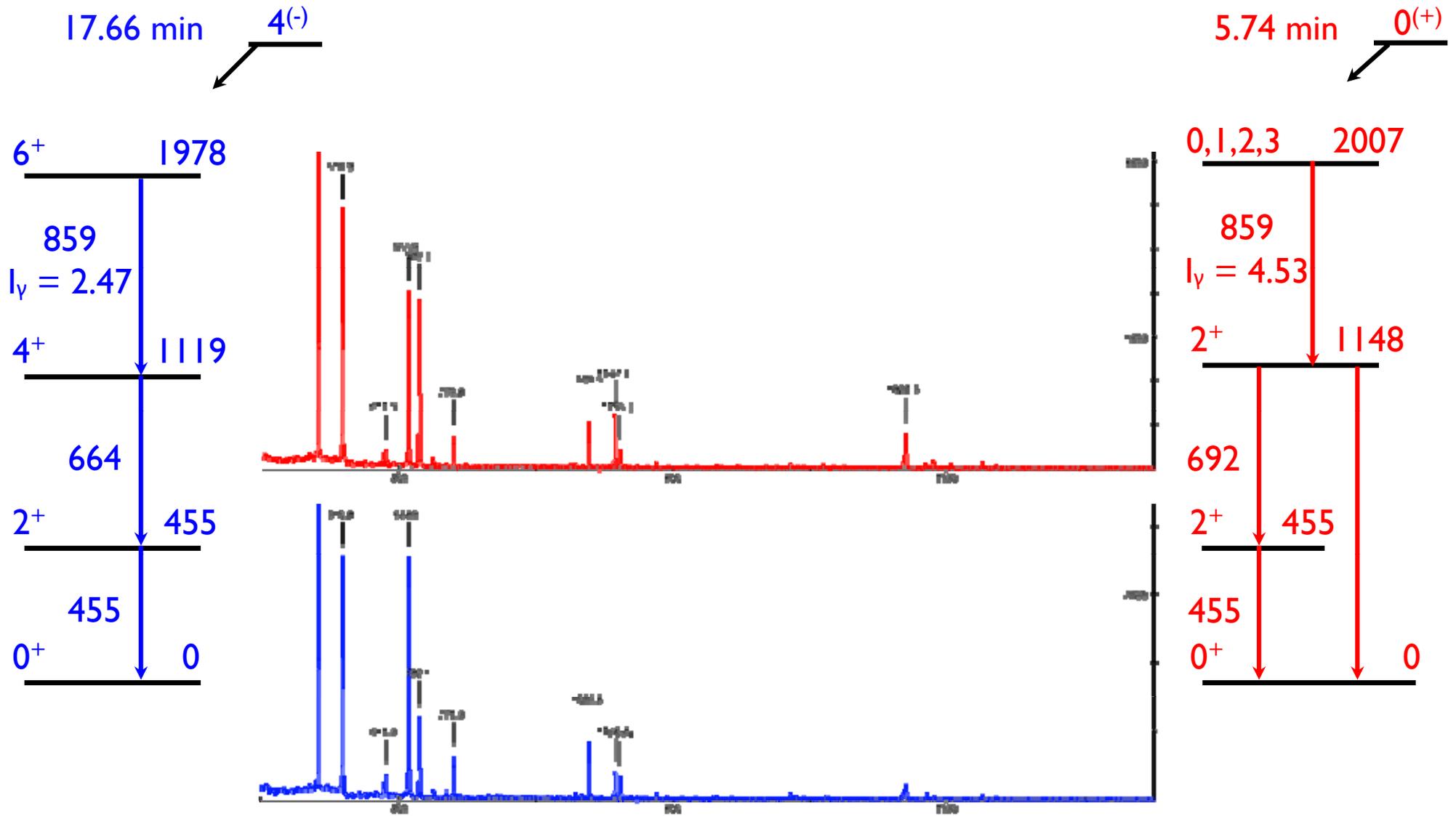


The **projection** of the  $\gamma$ - $\gamma$  coincidence matrix for 12 runs (~4 hours counting) and the **455-keV  $\gamma$ -gated spectrum**.

Sources were collected at the center of the  $8\pi$  for 40 seconds and counted for 20 minutes.

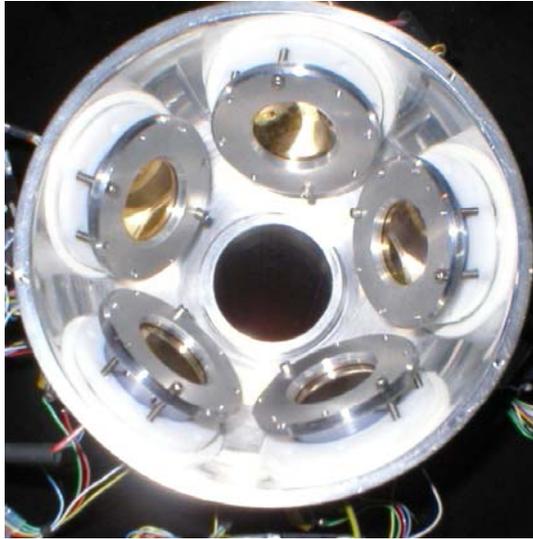


Isomer and ground-state decays were identified using the moving tape collector and varying the counting program.

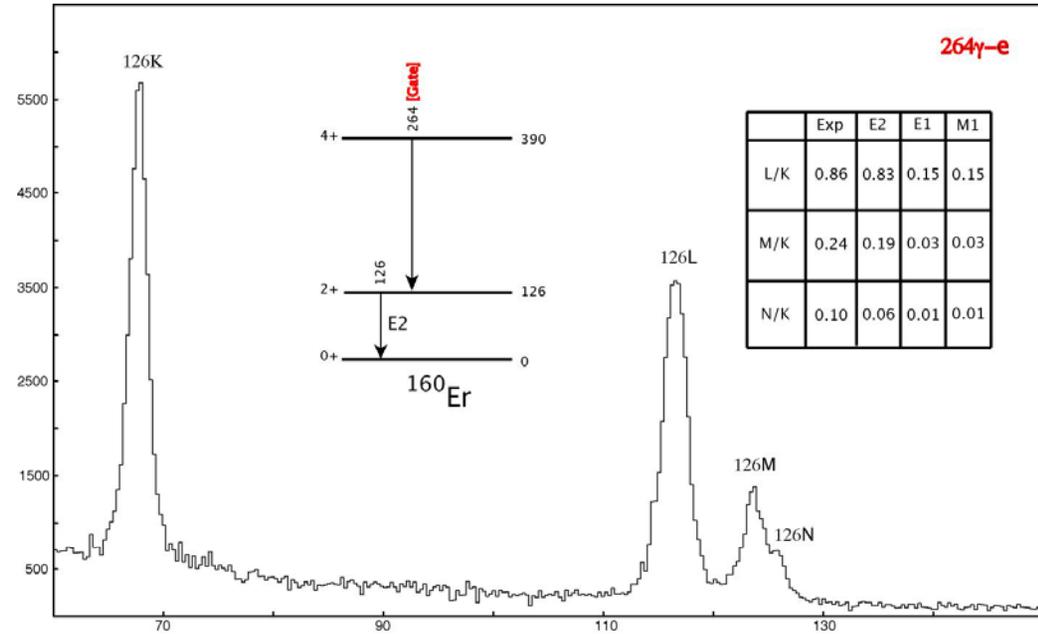
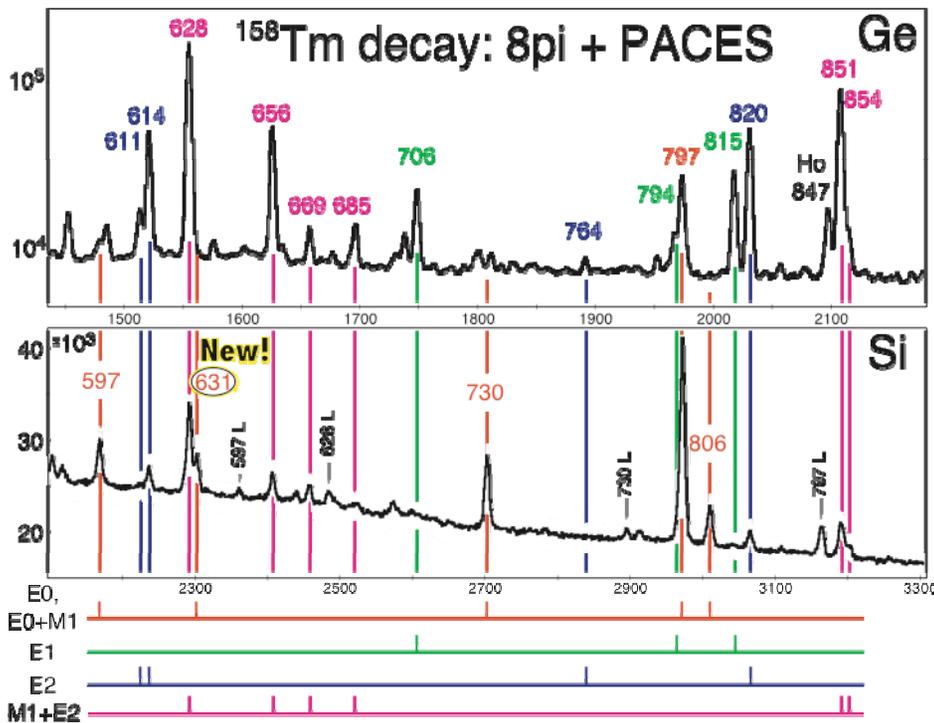


# Multipolarity information is extracted from PACES and $8\pi$ spectra.

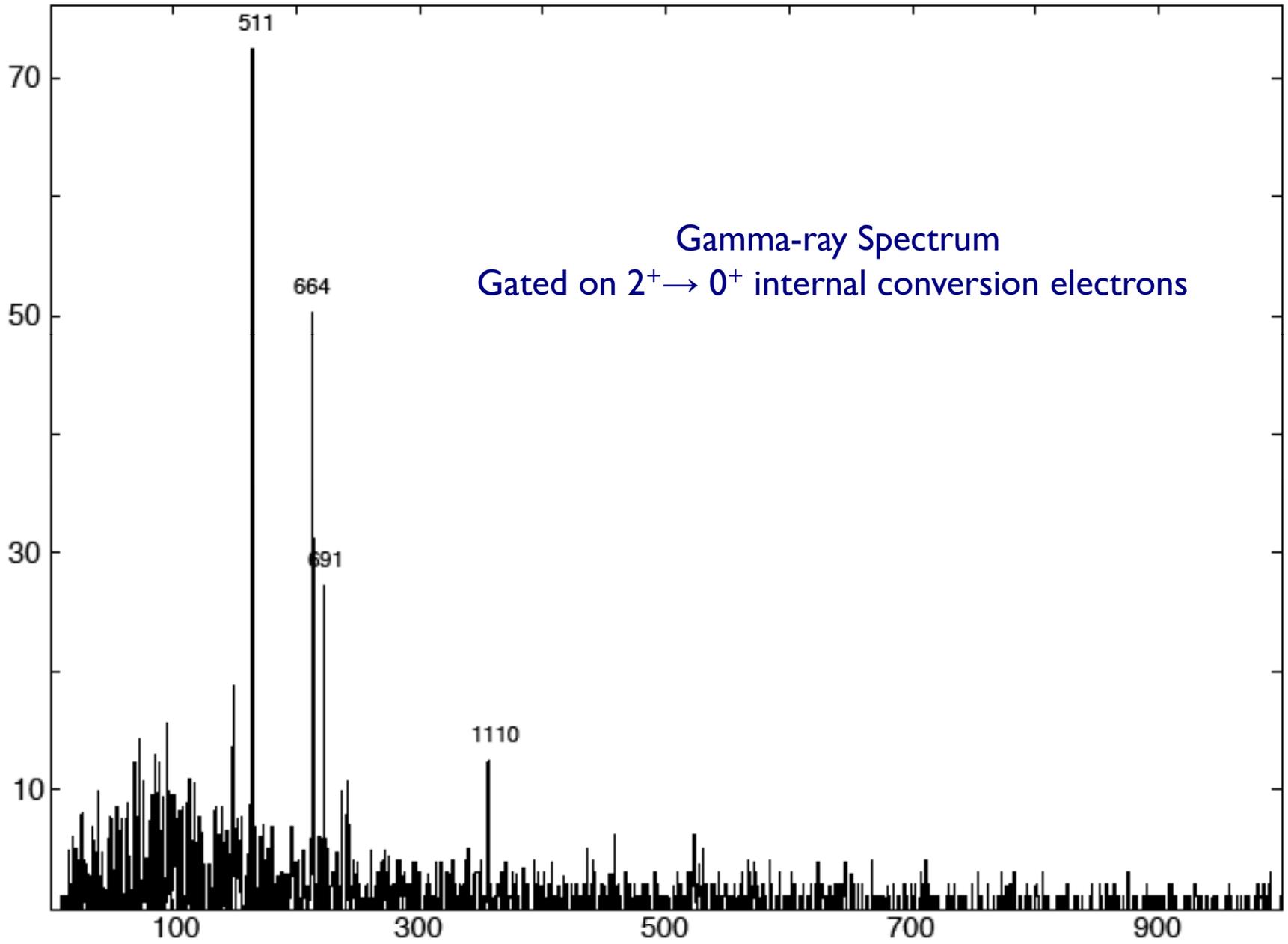
PACES, built by  
E. F. Zganjar  
(LSU)



Comparing EC/ $\gamma$  intensity provides  $\alpha_K$ .

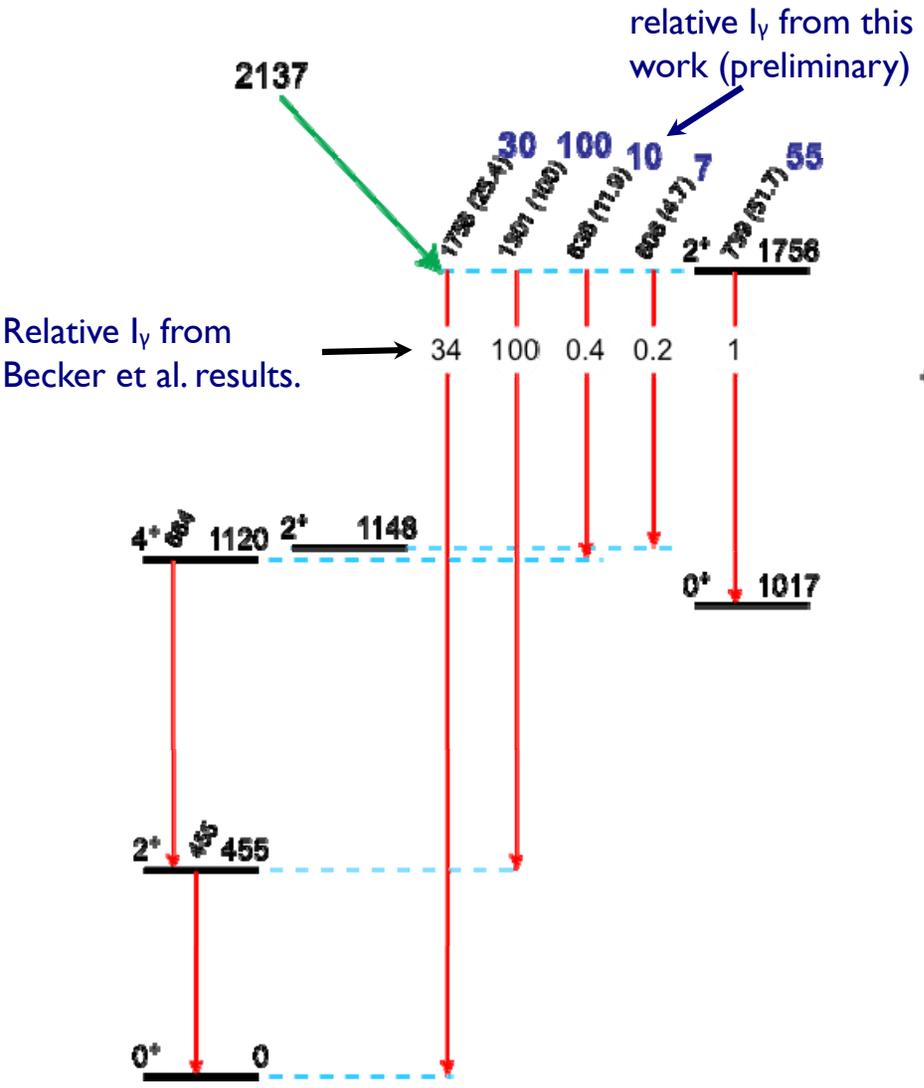
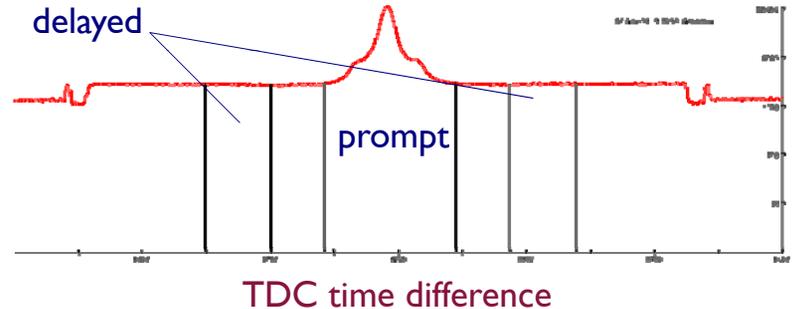


Subshell ratios provide multipolarity.  
Thesis work of N. Brown, Georgia Tech



Gamma-ray Spectrum  
Gated on  $2^+ \rightarrow 0^+$  internal conversion electrons

# Coincidence spectroscopy allows us to take clean cuts on the data for very specific interests.

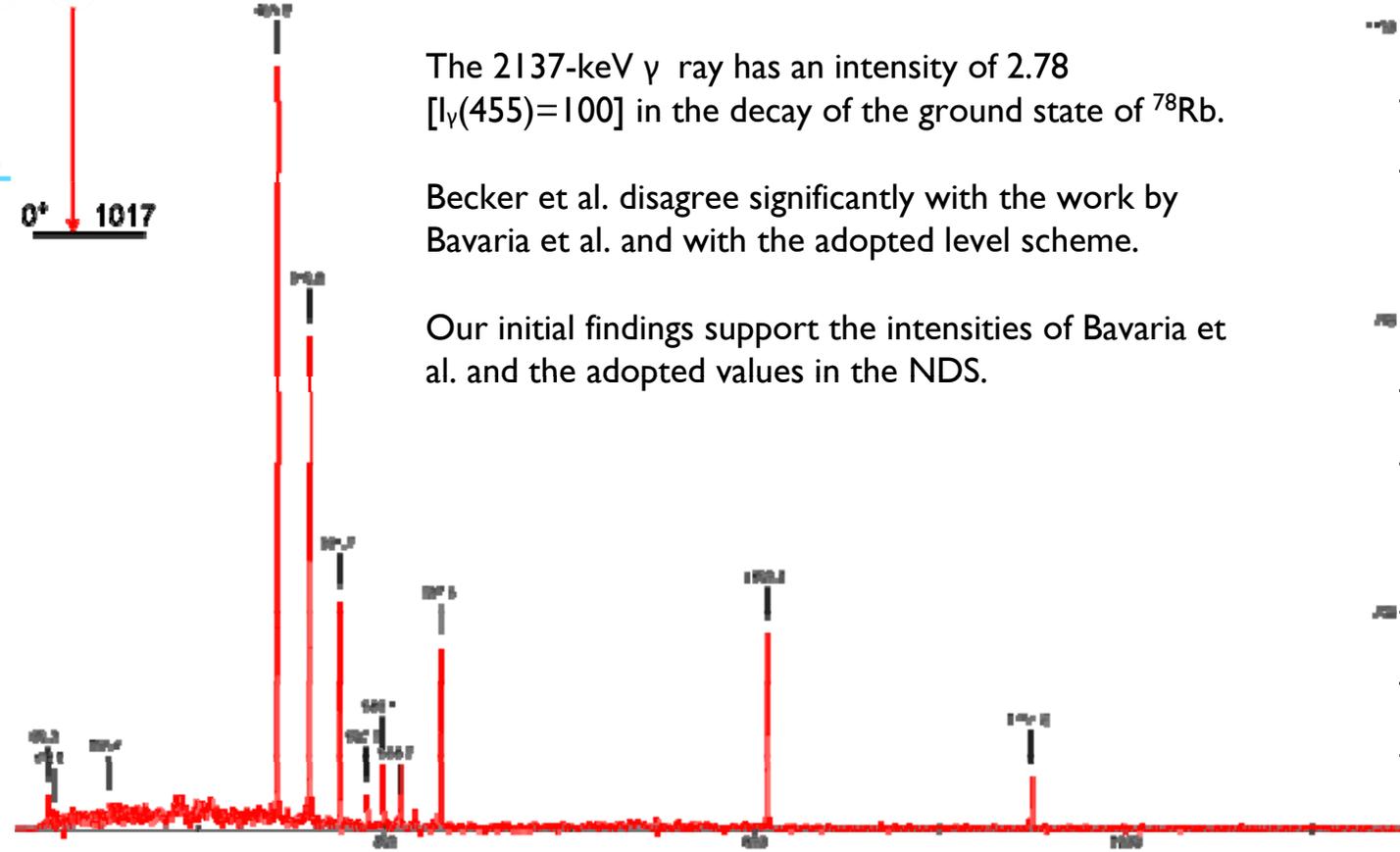


Key requirements are Compton suppression and removal of random coincidences.

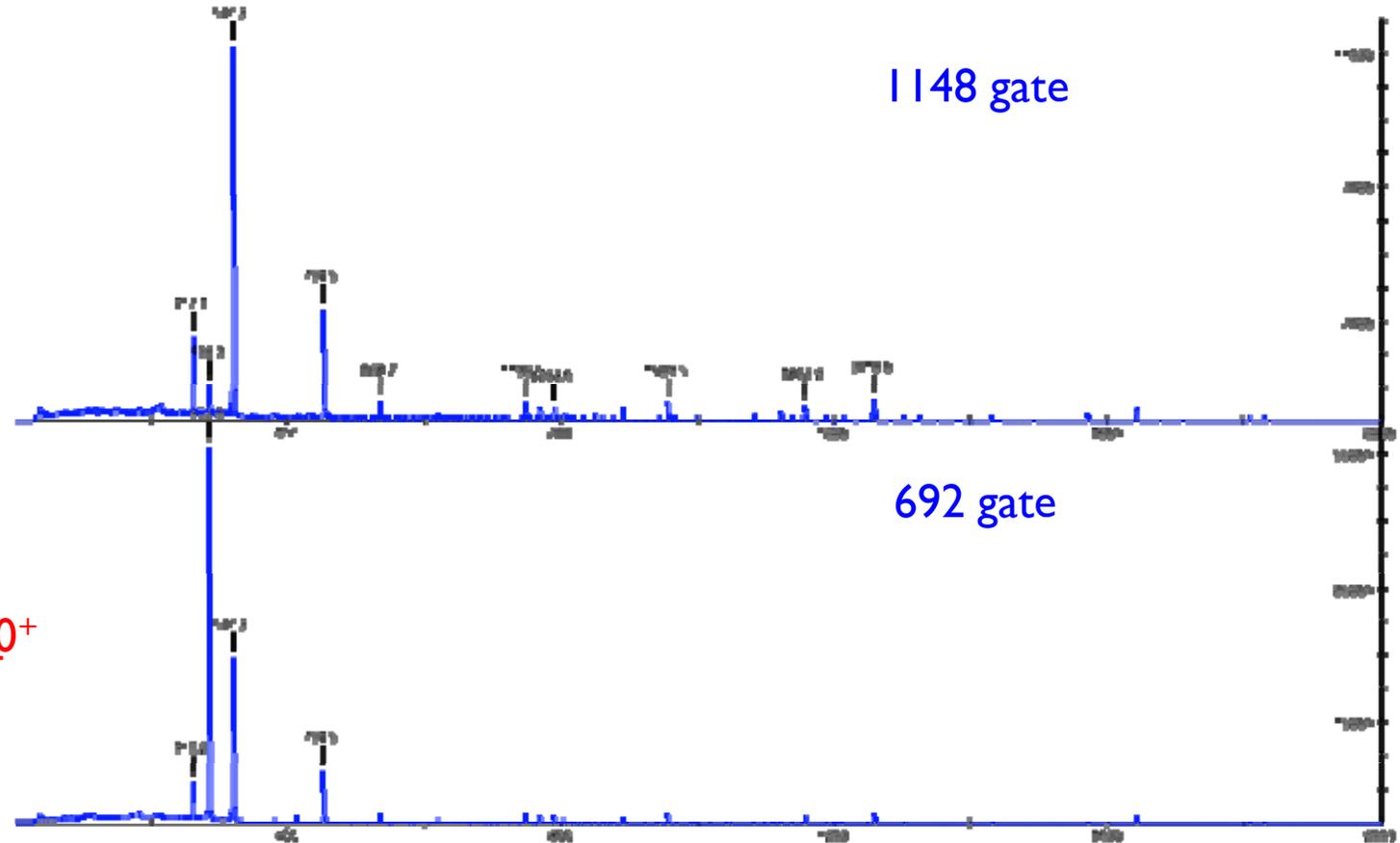
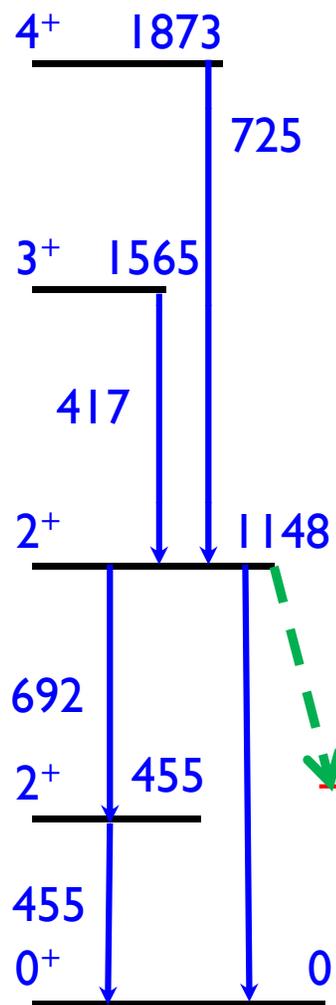
The 2137-keV  $\gamma$  ray has an intensity of 2.78 [ $I_\gamma(455)=100$ ] in the decay of the ground state of  $^{78}\text{Rb}$ .

Becker et al. disagree significantly with the work by Bavaria et al. and with the adopted level scheme.

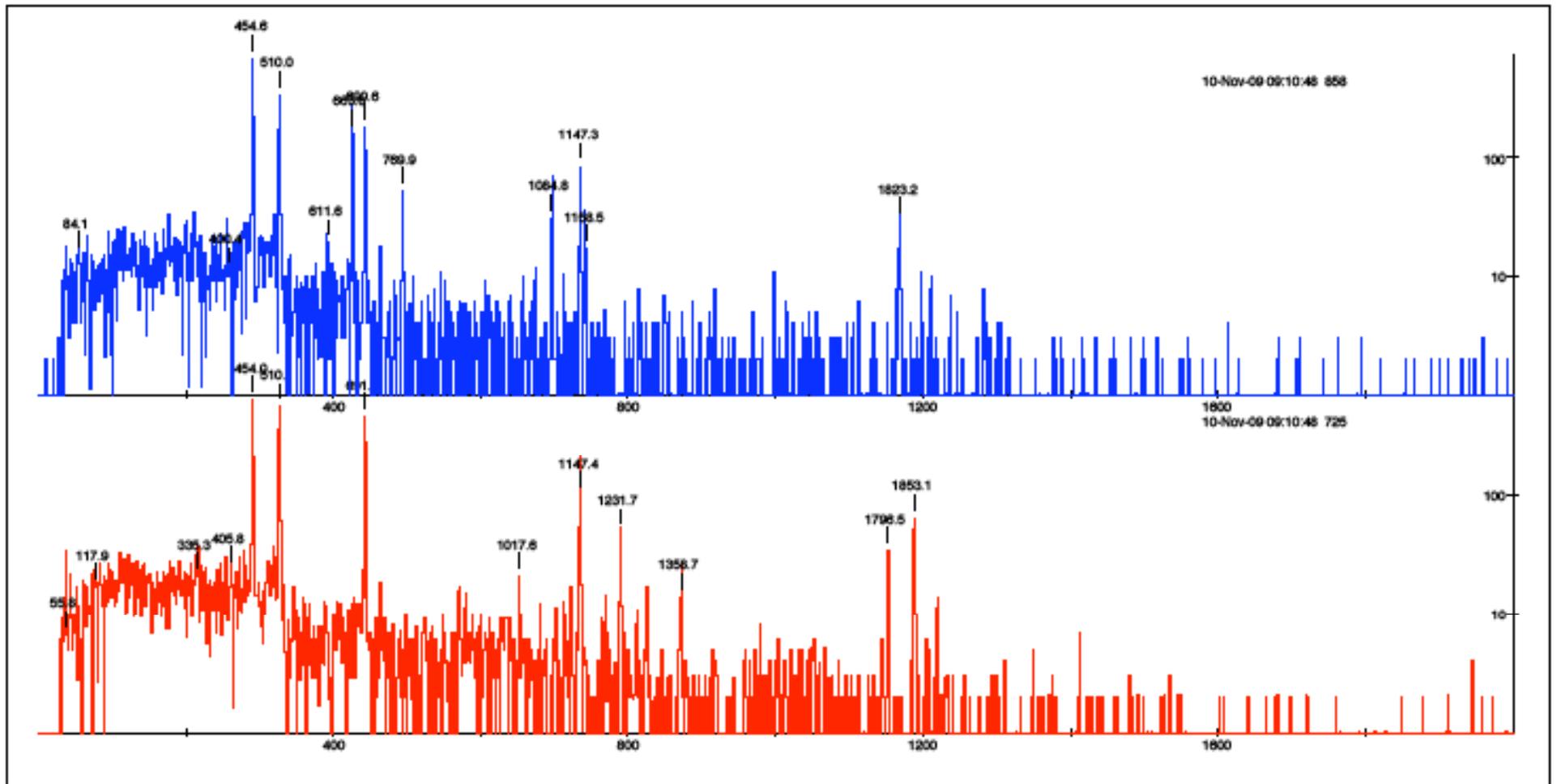
Our initial findings support the intensities of Bavaria et al. and the adopted values in the NDS.



The nature of the 1148-keV state ( $K=0$  or  $K=2$ ) will be determined from its band properties and detailed decay branching measurements.



# Gates on gamma-rays feeding the 1148-keV $2^+$ level



# Summary

- High-statistics data ( $\sim 1$  TB total) were collected for the decay of  $^{78\text{g,m}}\text{Rb}$  into  $^{78}\text{Kr}$ .
- Data analysis is underway on  $\gamma$ - $\gamma$ ,  $\gamma$ -e, e-e coincidence spectra (sorting continues).
- From these detailed spectroscopic measurements, we should:

identify the suggested, but yet to be identified  $0^+$  oblate bandhead (or set a stringent upper limit on its population).

determine  $B(\lambda)$  values for many transitions.

determine E0 components for  $I^\pi \rightarrow I^\pi$  transitions.

perform detailed spectroscopy of the low-energy, non-yrast structure of  $^{78}\text{Kr}$ .